



দ্য মরগ্যানের সূত্র (De Morgan's Law):

$$(A \cup B)' = A' \cap B'$$

$$(A \cap B)' = A' \cup B'$$

ধরি,  $x \in (A \cup B)'$

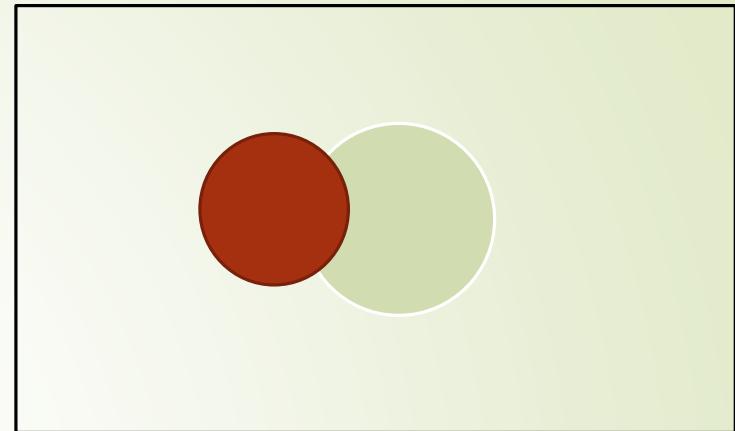
$$\Rightarrow x \notin (A \cup B)$$

$$\Rightarrow x \notin A \text{ এবং } x \notin B$$

$$\Rightarrow x \in A' \text{ এবং } x \in B'$$

$$\Rightarrow x \in (A' \cap B')$$

$$\therefore (A \cup B)' \subseteq (A' \cap B') \quad \dots \dots \dots \text{(i)}$$



আবার ধরি,  $x \in (A' \cap B')$

$$\Rightarrow x \in A' \text{ এবং } x \in B'$$

$$\Rightarrow x \notin A \text{ এবং } x \notin B$$

$$\Rightarrow x \notin (A \cup B)$$

$$\Rightarrow x \in (A \cup B)'$$

$$(A' \cap B') \subseteq (A \cup B)' \quad \dots \dots \dots \text{(ii)}$$

(i) ও (ii) হতে পাই,

$$\therefore (A \cup B)' \subseteq (A' \cap B')$$

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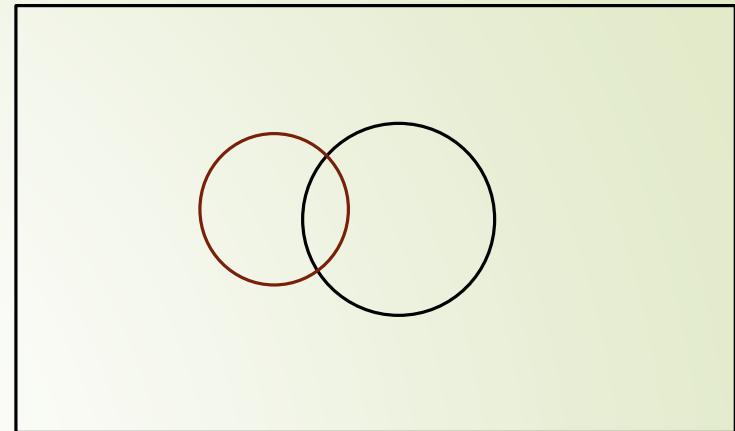
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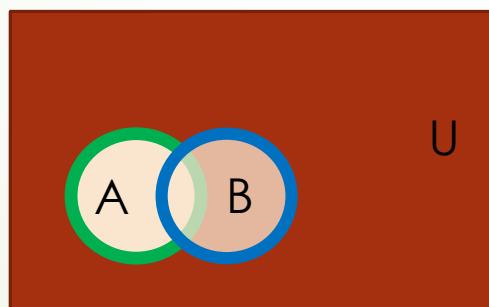
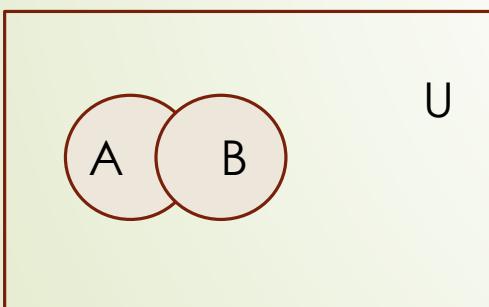
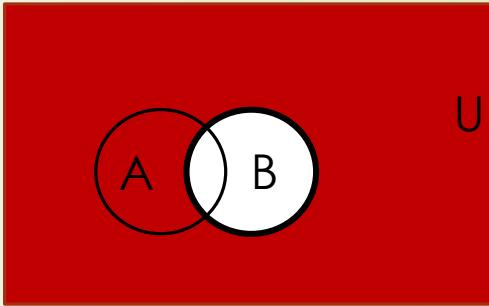
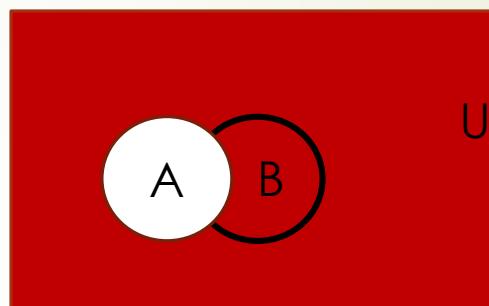
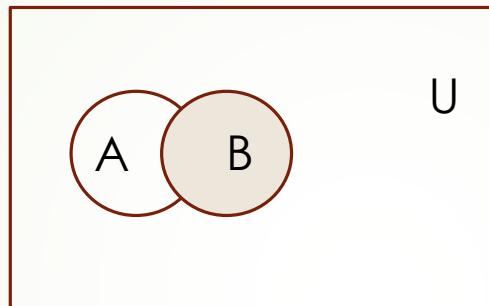
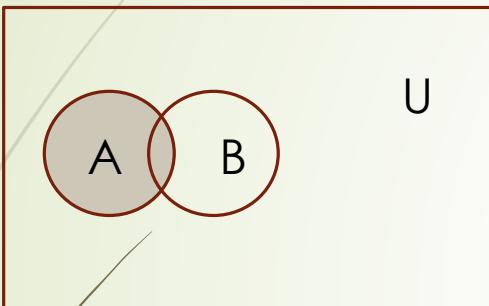
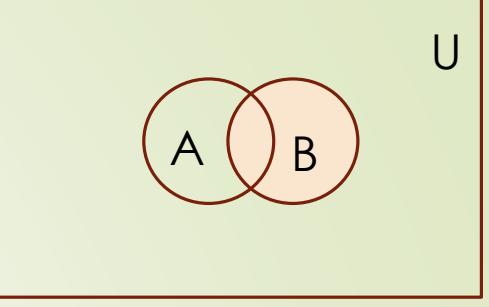
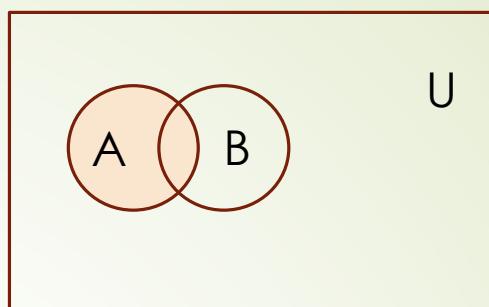
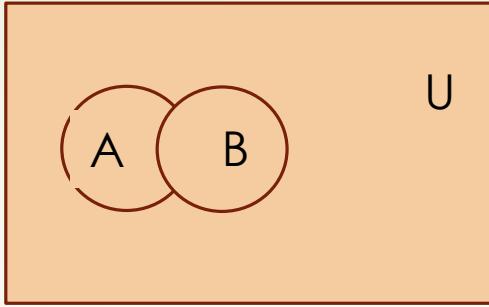
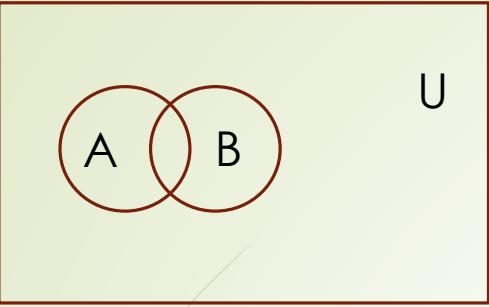
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$$\therefore (A \cup B)' \subseteq (A' \cap B')$$



$A \cup B$

$(A \cup B)'$

$A' \cap B'$